

Firm behavior during an epidemic

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Topics in Empirical Analysis and Economic Modeling Related to
COVID-19

FGV

Introduction

- Ongoing COVID-19 epidemic has claimed approx. 4 million lives
- Several economic and health impacts are related to firms
- Various policies targeting firms are being used worldwide
- Employee health is one of the main concerns of firms ([Bartik et al., 2020](#))
- This paper: study labor allocation behavior of firms in an epidemic environment and how that can affect the dynamics of the epidemic

This paper

Structural model of firm behavior and disease transmission

- Firms
 - Maximizes discounted profits
 - Workers → on-site, teleworking, furlough, sick-leave
 - Infectious workers transmit disease in the workplace
 - Firm internalizes this
- General equilibrium
 - Distribution of workers across health statuses determine aggregate infectiousness
- Calibration: COVID-19 in the U.S.

Preview of results

- Firm fights infections
 - Teleworking
 - Weekly rotation: on-site work \leftrightarrow telework (two groups)
 - Flattens aggregate infection curve
- Subsidies to sick-leave reduce cost of sick worker \rightarrow more deaths
- Furlough policies and subsidies to teleworking save lives
- Firm delays the fight against infection during economic downturns
- Planner adopts no-COVID strategy if vaccine arrives in 1.5 years

Model

- Time is discrete and runs forever
- Continuum of identical firms
- Firms choose allocation of employees
- Workforce of the firm
 - On-site employees (more productive, higher risk)
 - Teleworking (remote) employees (less productive, lower risk)
 - Employees on leave (furloughed)
 - Employees on sick leave
- On-site infectious employees transmit to susceptible on-site employees
- Firm takes workplace transmission into account
- Firm takes infection outside of the workplace as given

Model

- Production function of firm is

$$f(n, h) = A(n + \gamma h)^\alpha, \quad A > 0, \alpha, \gamma \in (0, 1) \quad (1)$$

- n : mass of on-site workers
- h : mass of teleworkers
- Per-period profit of the firm is

$$\pi(n, h, \ell, s) = f(n, h) - \delta_n wn - \delta_h wh - \delta_\ell w\ell - \delta_s ws \quad (2)$$

- ℓ : mass of workers on leave
- s : mass of symptomatic sick workers
- δ : relative cost/policy parameters
- w : wage, parameter

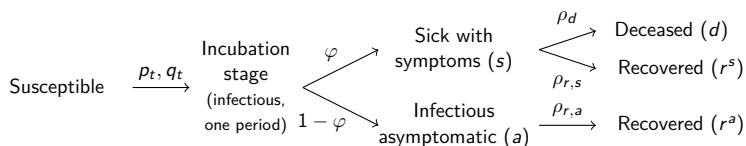
World before the epidemic

- N : number of workers in the no-disease scenario

$$N = \operatorname{argmax}_n An^\alpha - \delta_n wn \quad (3)$$

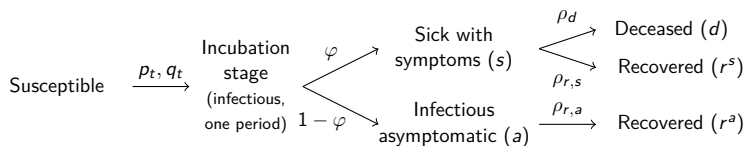
- Disease arrives unexpectedly
- No hiring/firing after disease arrives

Infections and health states

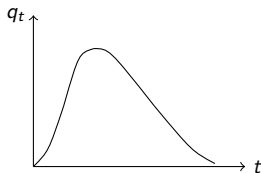


- q_t : probability of an employee getting infected if not on-site in t
 - Firm takes $\{q_t\}_t$ as given
- $p_t(\mu)$: probability of infection in t if on-site and there are μ infectious on-site employees
 - Firm internalizes its effect on p_t

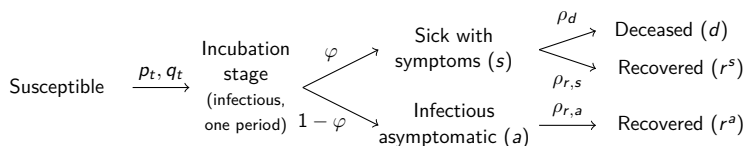
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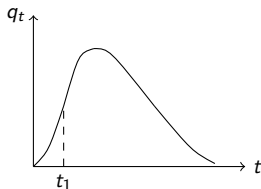
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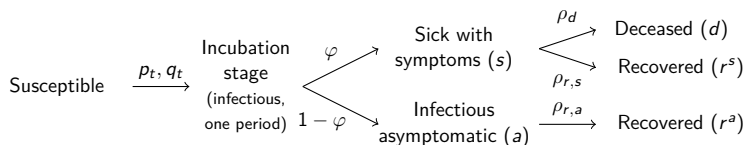
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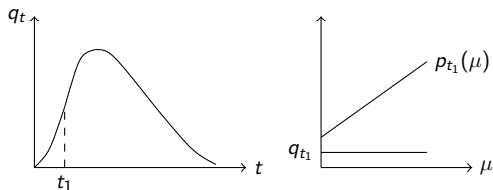
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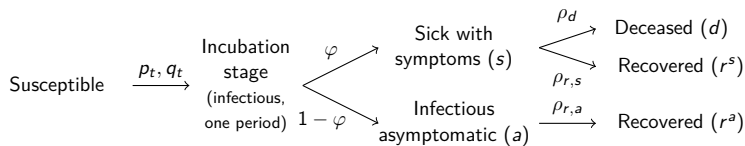
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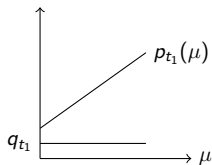
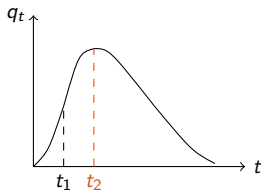
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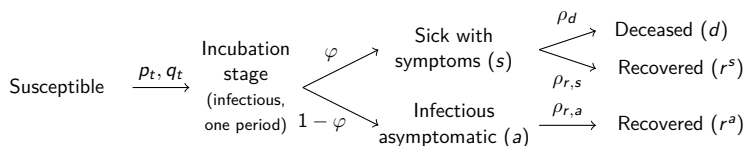
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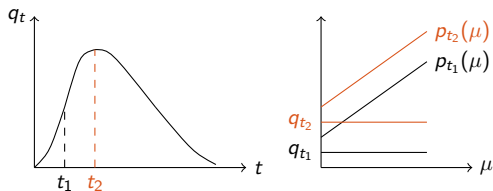
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Human resources by health status

- Firm observes four groups of workers:
 1. Deceased
 2. Sick symptomatic
 3. Recovered symptomatic
 4. Employees with uncertain health status
 - 4.1 Susceptible
 - 4.2 Incubated infection (infectious)
 - 4.3 Infectious asymptomatic
 - 4.4 Recovered asymptomatic

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Which groups can the firm manage?

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Human resources by health status

- Firm observes four groups of workers:
 1. Deceased
 2. Sick symptomatic
 3. Recovered symptomatic
 4. Employees with uncertain health status $\left\{ \begin{array}{l} \text{On-site in } t - 1 \\ \text{Not on-site in } t - 1 \end{array} \right.$
 - 4.1 Susceptible
 - 4.2 Incubated infection (infectious)
 - 4.3 Infectious asymptomatic
 - 4.4 Recovered asymptomatic

Which groups can the firm manage?

Last ingredients

- Choice variables:

		On-site in t	Teleworker in t	Furlough in t
Uncertain status	On-site in $t - 1$	n_t^n	h_t^n	ℓ_t^n
	Not on-site in $t - 1$	n_t^m	h_t^m	ℓ_t^m
Recovered workers		n_t^r	h_t^r	ℓ_t^r

- Firm knows laws of motion of the disease
- Firm uses law of large numbers to know distribution of workers across all health states
- Firm maximizes discounted profits
- Initial condition: ε mass of workers in incubation stage

▶ All equations

General equilibrium

- Firm takes as given the path of q_t
- q_t is determined in equilibrium by the firms' choices

$$q_t = \Pi_q [\text{n. of workers in incubation stage in } t + \text{n. of asymptomatic sick workers in } t] \quad (4)$$

where $\Pi_q > 0$

► Features of the model

► Calibration

Benchmark equilibrium

Figure: The dynamics of the epidemic

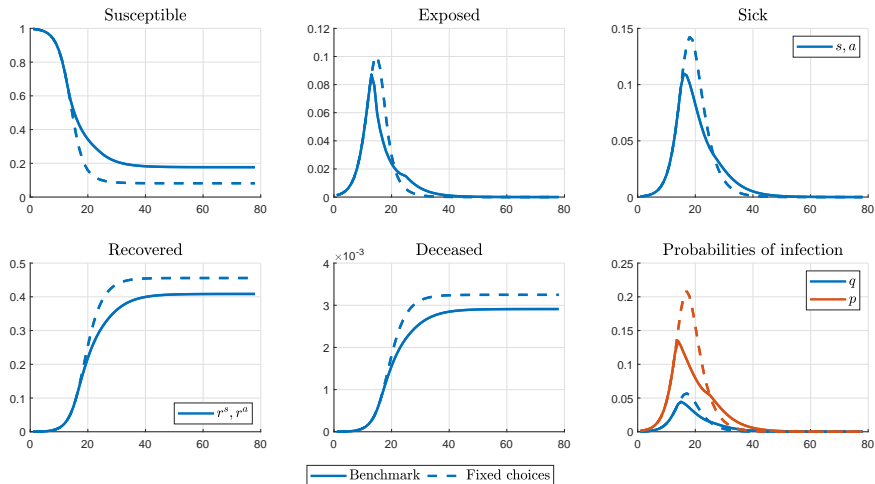


Figure: The dynamics of employee allocations during the epidemic

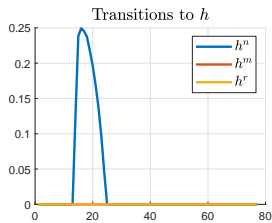
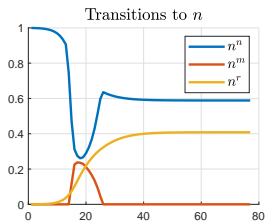
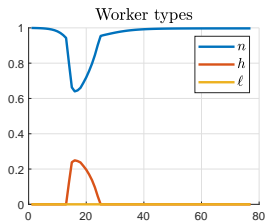


Table: Benchmark equilibrium, “epidemiological” model, and policies

	Benchmark	Fixed choices	Teleworking $\delta_h = 0.975$	Sick leave $\delta_s = 0$	Furlough $\delta_\ell = 0$
Weeks to the peak	15	17	14	17	16
Sick at the peak (%)	10.96	14.25	7.62	14.25	8.31
Deceased (%)	0.29	0.32	0.26	0.32	0.27
Deceased (% Δ w.r.t. BM)	0.00	11.54	-10.01	11.54	-8.27
Recovered (%)	82.01	91.47	73.81	91.47	75.23
Recovered (% Δ w.r.t. BM)	0.00	11.54	-10.01	11.54	-8.27
Production 1 year (% Δ w.r.t. ND)	-2.26	-2.34	-2.24	-2.34	-7.19
Production 1 year (% Δ w.r.t. BM)	0.00	-0.09	0.02	-0.09	-5.04
Discounted profits	381.20	381.17	381.26	382.28	381.25
Discounted profits (% Δ w.r.t. ND)	-0.29	-0.29	-0.27	0.00	-0.27
Discounted profits (% Δ w.r.t. BM)	0.00	-0.01	0.02	0.28	0.01
Profits 1 year (% Δ w.r.t. ND)	-7.11	-7.32	-6.59	-0.11	-6.77
Profits 1 year (% Δ w.r.t. BM)	0.00	-0.23	0.56	7.54	0.37
Max. teleworking (%)	24.97	0.00	32.24	0.00	17.80
Max. leave (%)	0.00	0.00	0.00	0.00	14.70
Max. n to m (%)	24.97	0.00	32.24	0.00	28.32
Max. m to n (%)	23.81	0.00	31.25	0.00	27.39
Sum n to m	1.95	0.00	4.74	0.00	4.92
Sum m to n	1.88	0.00	4.64	0.00	4.83

Notes: “BM”: benchmark. “ND”: no-disease.

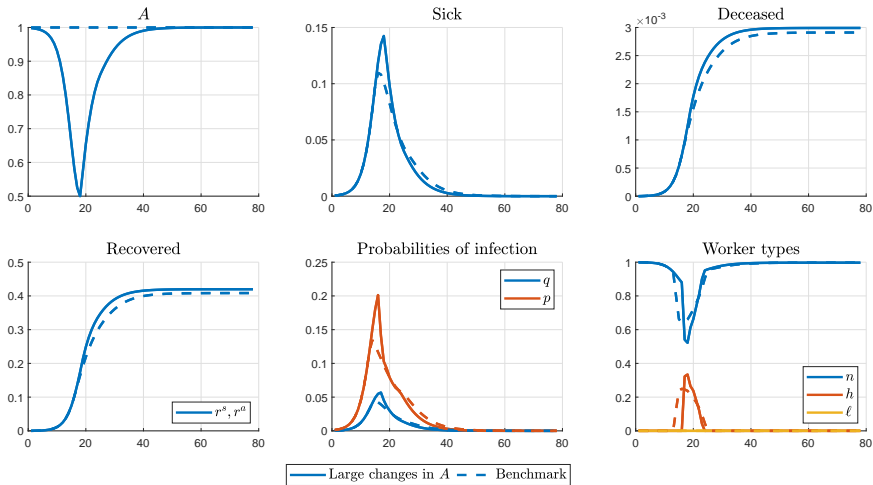
Production restrictions, changes in the demand, and lockdowns

- Reduced form approach for production restrictions, fall in demand (Fernández-Villaverde and Jones, 2020)
- If more sick individuals, lower demand:

$$A_t = 1 - \delta_A s_t \quad (5)$$

- (Atomistic) firm doesn't internalize this

Figure: Large changes in A



Firm delays teleworking during the economic downturn.

Why?

- Surprising? One expectation could be:

During downturn, marginal revenue is lower

⇒ Foregone revenue of teleworker is lower

⇒ Firm protects workers

- What actually happens:

- Revenue brought by on-site/teleworker doesn't vary across time:

$$\frac{\text{Mg. rev. of on-site worker in } t}{\text{Mg. rev. of teleworker in } t} = \frac{A_t \times 1}{A_t \times \gamma} = \frac{1}{\gamma} \quad (6)$$

- Relative costs of different types of workers don't change
- Opportunity cost of having a sick worker changes over time:

Foregone revenue of sick worker in t is proportional to A_t

Firm delays teleworking during the economic downturn. Why?

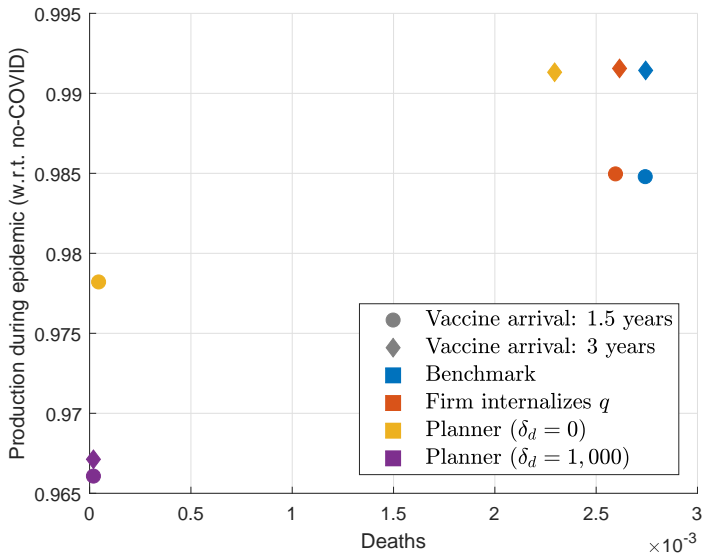
- Opportunity cost of sick worker falls in the COVID outbreak
- Disease is not so deadly for young workers
- Firm wants recovered workers when demand starts moving up
- Firm prefers infections in the beginning rather than in the end
- This aggravates the economic downturn and the infection spike

A planner

- Planner's objective function:

$$\sum_{t=0}^{\infty} \beta^t [f(n_t, h_t) - \delta_d(d_t - d_{t-1})] \quad (7)$$

- δ_d captures non-pecuniary value of life
- Planner internalizes the effect of its choices on q
- Constrained by laws of motion of the disease



Conclusions

- Novel model where firms operate in an epidemic environment
- Model is calibrated to the COVID-19 in the US
- Firms' choices have significant effects on the epidemic
- Policies can have considerable impacts on the epidemic
- Firms don't fight epidemic in economic downturns
- Planner adopts no-COVID strategy if vaccine arrives in 1.5 years

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Appendix

Literature

Pre-COVID

- Theory
 - Kremer (1996), Chen et al. (2011), Toxvaerd (2019)
 - Infected agents impose **negative externalities** on susceptible by not internalizing the costs of transmission
- Quantitative
 - Chan et al. (2016), Greenwood et al. (2019)
 - The role of this externality in quantitative economic models of disease transmission
- Our contribution
 - Firms **internalize** some of these externalities...
 - ... with a different objective function (profits)

Literature

Post-COVID

- Structural models with COVID-19 transmission:
 - Alvarez et al. (2020), Acemoglu et al. (2020), Brotherhood et al. (2020a,b), Eichenbaum et al. (2020a,b), Glover et al. (2020), Guerrieri et al. (2020), Kaplan et al. (2020), and others
 - Optimal containment policies, importance of behavior, testing, macroeconomic stabilization policies...
 - Common aspect of all: focus on modeling workers
 - Our contribution: first paper modeling firms in an environment with disease transmission
- Empirical papers assessing impacts on firms:
 - Alfaro et al. (2020), Bartik et al. (2020), Ding et al. (2020), Fahlenbrach et al. (2020), Hassan et al. (2020)

Laws of motion

$$d_{t+1} = d_t + \rho_d s_t \quad (8)$$

$$r_{t+1}^s = r_t^s + (1 - \rho_d)\rho_{r,s}s_t \quad (9)$$

$$r_{t+1}^a = r_t^a + \rho_{r,a}a_t \quad (10)$$

$$s_{t+1} = (1 - \rho_d)(1 - \rho_{r,s})s_t + \varphi(\tilde{n}_t + \tilde{m}_t) \quad (11)$$

$$a_{t+1} = (1 - \rho_{r,a})a_t + (1 - \varphi)(\tilde{n}_t + \tilde{m}_t) \quad (12)$$

- \tilde{n}_t : on-site employees with incubated infection in t
- \tilde{m}_t : out of workplace employees with incubated infection in t

- $a_{n,t}$: on-site asymptomatic employees (infectious) in t

$$a_{n,t} = (n_t^n + n_t^m) \frac{a_t}{N - r_t^s - s_t - d_t} \quad (13)$$

- Probability of infection of on-site employees

$$p_t = \min \{ \Pi_{p,q} q_t + \Pi_{p,n} (\tilde{n}_t + a_{n,t}), 1 \} \quad (14)$$

where $\Pi_{p,q} \geq 1$ and $\Pi_{p,n} > 0$

- c_{t-1} : fraction of susceptible among uncertain workers in $t - 1$

$$c_{t-1} = 1 - \frac{r_t^a + a_t}{N - r_t^s - s_t - d_t} \quad (15)$$

- Laws of motion for \tilde{n}_t and \tilde{m}_t

$$\tilde{n}_t = n_t^n c_{t-1} p_{t-1} + n_t^m c_{t-1} q_{t-1} \quad (16)$$

$$\tilde{m}_t = (h_t^n + \ell_t^n) c_{t-1} p_{t-1} + (h_t^m + \ell_t^m) c_{t-1} q_{t-1} \quad (17)$$

Constraints

- Workers in each group must be split among available options:

$$n_t^n + h_t^n + \ell_t^n = n_{t-1}^n + n_{t-1}^m - \varphi \tilde{n}_{t-1} \quad (18)$$

$$n_t^m + h_t^m + \ell_t^m = h_{t-1}^n + \ell_{t-1}^n + h_{t-1}^m + \ell_{t-1}^m - \varphi \tilde{m}_{t-1} \quad (19)$$

$$n_t^r + h_t^r + \ell_t^r = r_t^s \quad (20)$$

- Initial conditions:

$$n_{-1}^n = N, \quad \tilde{n}_{-1} = \varepsilon \quad (21)$$

all else zero

- ε : initial mass of infected workers

Firm's problem

- Firm maximizes

$$\sum_{t=0}^{\infty} \beta^t \pi_t \quad (22)$$

subject to constraints and laws of motion

- Choice variables:

$$n_t^n, h_t^n, \ell_t^n, n_t^m, h_t^m, \ell_t^m, n_t^r, h_t^r, \ell_t^r \geq 0 \quad \forall t \quad (23)$$

Two-stage problem

- All dynamic equations that depend on h and ℓ only depend on these variables through $h + \ell \equiv m$.
- Static problem: for a given n and m ,

$$\max_{h, \ell \geq 0} A(n + \gamma h)^\alpha - \delta_n wn - \delta_h wh - \delta_\ell w\ell - \delta_s ws \quad (24)$$

$$\text{subject to } h + \ell = m \quad (25)$$

- Choice variables of dynamic problem:

$$n_t^n, m_t^n, n_t^m, m_t^m, n_t^r, m_t^r \geq 0 \quad \forall t \quad (26)$$

Features of the model

- The epidemic has negatives effects on output and profits
 - Workforce shrinks: employees catch infection and take a sick leave
 - Fall in output and profits since $\delta_s > 0$ and the firm cannot achieve its optimal size
 - Workforce is smaller after the culmination of the epidemic because of fatalities
 - This also reduces output and profits
- All known recovered employees are allocated on-site
- Decreasing returns to scale technology
 - Firm wants to smooth infections over time

Features of the model

- Firm wants to allocate employees into teleworking and leave in times of an epidemic
 - These reduce p_t and infections among all employees given that $p_t \geq q_t$
- Dynamic trade-offs:
 - On-site workers:
 - Higher output in the present and in the “distant” future
 - Sick-leave, fatality
 - Teleworking employees:
 - Lower productivity
 - Lower infection probability
- Incentives to rotate employees between on-site work and teleworking
 - On-site worker in $t - 1$ has higher probability of being infectious in t

Calibration

Parameter	Value	Comment
Panel A. Firm		
A	1	Normalization
N	1	Normalization
α	0.7	Labor share of revenues
β	$0.96^{1/52}$	Time discount (weekly)
γ	0.935	$\approx 30\%$ in teleworking at peak (Brynjolfsson et al., 2020)
w	0.7	Wage is such that optimal $N = 1$ in no disease/epidemic times
$\delta_n, \delta_h, \delta_\ell, \delta_s$	1	Policy parameters
Panel B. COVID-19		
$\rho_{r,s}$	1/3.52	Average duration of hospitalization (Verity et al., 2020)
$\rho_{r,a}$	1/3.52	Same as $\rho_{r,s}$
ρ_d	0.00202	Probability of death conditional on hospitalization (CDC, 2020)
Π_q	0.25	$R_0 = 2.5$
$\Pi_{p,q}$	1	No discontinuity from q to p
$\Pi_{p,n}$	0.6667	$\approx 50\%$ transmissions in the workplace at peak (Ferguson et al., 2006)
φ	0.5	Proportion of asymptomatic, range: 4%-75% (CEBM, 2020)
ε	0.001	0.1% infected workers in first period
Panel C. Time		
Time period	1 week	
Epidemic end	1.5 years	Deterministic vaccine arrival