Fair Allocation of Vaccines, Ventilators and Antiviral Treatments: Leaving No Ethical Value Behind in Health Care Rationing

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Brazilian School of Economics October 8, 2020

Synopsis

- COVID-19 pandemic has spurred renewed interest in guidelines for rationing scarce medical resources.
 - Guidelines written for a wide range of public health emergencies.
 - Scarce items: ventilators, ICU beds, anti-virals, vaccines, etc.
- The most widespread allocation mechanism is based on a priority system, which places patients into a single priority order and allocates all units based on this priority.

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- The most widespread allocation mechanism is based on a priority system, which places patients into a single priority order and allocates all units based on this priority.
- This paper:
 - 1) We argue a priority system is too restrictive; we show how existing guidelines struggle to integrate or balance ethical considerations.
 - 2) To increase flexibility, we propose and analyze a reserve system.
 - 3) We develop a general theory of reserve design, introduce cutoff equilibrium, smart reserves, and extend sequential reserve matchings.
 - 4) We relate these concepts to current debates.

Background

- COVID-19 pandemic has motivated policymakers to revisit existing or issue new guidelines on allocating medical resources (Emanuel et al. NEJM 2020, Truog et al. NEJM 2020).
- These guidelines appeal to various ethical principles including:
 - Saving the most lives
 - Saving the most life-years
 - The life-cycle principle

- Instrumental value
- Reciprocity
- Equal access

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 - Saving the most life-years
 - The life-cycle principle

- Instrumental value
- Reciprocity
- Equal access
- These principles can compete with one another:
 - E.g., equal access ignores patient age while the life-cycle principle explicitly considers it.
- An allocation mechanism must implement the desired balance of ethical values.

Ethical Value of Saving the Most Lives: SOFA Score

- For some of these principles,
 - only individual attributes are relevant, and
 - they either have a natural or a well-established cardinal measure.
- Metric for life-cycle principle: Age
- Metric for saving the most lives: Sequential Organ Failure Assessment (SOFA) score

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- Metric for life-cycle principle: Age
- Metric for saving the most lives: Sequential Organ Failure Assessment (SOFA) score
- The SOFA score numerically quantifies the number and severity of failed organs: Each of six organ groups lungs, liver, brain, kidneys, blood clotting and blood pressure is assigned a score of 1 to 4, with higher scores for more severely failed organs.
- The total SOFA score is shown to be useful in predicting the clinical outcomes of critically ill patients.

CDC Priority System for Vaccines from 2018

- Place individuals into one of four tiers based on:
 - 1) Providing homeland and national security
 - 2) Providing health care and community support services
 - 3) Maintaining critical infrastructure
 - 4) Being a member of the general population

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- Place individuals into one of four tiers based on:
 - 1) Providing homeland and national security
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 - 4) Being a member of the general population
- Currently, there is a vigorous debate on vaccine allocation.
- Melinda Gates in June 2020:

"We care about this vaccine getting out equitably. The first people that need this vaccine are the 60 million health care workers around the world. They deserve to get it before anybody else. Then you start tiering. In the U.S. that would be black people next, quite honestly, and many other people of color. They are having disproportionate effects from Covid-19."

Limitation: Inability to Accommodate Compromises

Who should get coronavirus vaccine first? U.S. weighs early access for some

July 9, 2020 at 4:45 am | Undated July 9, 2020 at 7:51 am



Dr. Francis Collins, director of the National Institutes of Health
(NIH), holds up a model of COVID-19 during a Senate hearing on
the plan to research. (Swill peb / The Associated Press) More...

By Megan Twohey

The New York Times

Federal health officials are already trying to decide who will get the first doses of any effective coronavirus vaccines, which could be on the market this winter but could require many additional months to become widely available to Americans.

The Centers for Disease Control and Prevention and an advisory committee of outside health experts in April began working on a ranking system for what may be an extended rollout in the United States. According to a preliminary plan, any approved vaccines would be offered to vital medical and national security officials first, and then to other essential workers and those considered at high risk—the elderly instead of children, neonle with underlying conditions instead of the relatively healthy.

Agency officials and the advisers are also considering what has become a contentious option: putting Black and Latino people, who have disproportionately fallen victim to COVID-19, ahead of others in the population.

The lunatic drive for racial quotas for COVID-19 vaccines

July 16, 2020 | 7:38pm



At least two COVID-19 vaccines are scoring major successes in trials.

Sign up for our special edition newsletter to get a daily update on the coronavirus pandemic

At least two COVID-19 vaccines are scoring major successes in trials. That means a vaccine might be ready by year's end, but not in sufficient quantity to vaccinate more than 300 million Americans. Frontline health workers and national-security presponsel will be no nicidity but after that who comes pend?

A federal committee is considering pushing blacks, Hispanics and Native Americans to the front of the line, ahead of whites.

Single-Principle vs. Multi-Principle Priority Point Systems

- The SOFA score is considered a good proxy for mortality risk.
- So if the sole ethical value under consideration is the utilitarian goal of saving the most lives, a single-principle point system based on SOFA scores may be a good choice.
- But if there are multiple ethical values, and many argue that should be the case, then a priority point system is too restrictive to reach an ethically-compelling balance between the desired values.
- It maps individual attributes to a numeric scale, and therefore cannot even incorporate principles which lack a cardinal and monotonic representation, let alone aggregate them.

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- It maps individual attributes to a numeric scale, and therefore cannot even incorporate principles which lack a cardinal and monotonic representation, let alone aggregate them.
 - Example: It cannot accommodate distributional objectives such as proportional representation of disadvantaged groups.

Example for Science Fiction Fans: Doomsday Scenario

- Consider a future pandemic so devastating that it threatens a significant portion of the human race.
- In this hypothetical crisis, a principle based on survival of the species may suggest a gender balance constraint: Assign at least 40% of the ventilators to female patients and at least 40% to male patients.
- Clearly, considerations based on group composition cannot be represented with a function that relies on individual attributes only.

Emergence of the Point Systems in the US

- While recognizing the need to consider multiple ethical values, many states adopted a priority point system based on SOFA scores only.
- Others have adopted multi-principle point systems to accommodate multiple ethical values.
- For ventilator allocation, the point system emerged as the mechanism of choice in the US, adopted in the following states:
 - Single-Principle Point System: NY, MN, NM, AZ, NV, UT, CO, OR, IN, KY, TN, KS, VT
 - Multi-Principle Point System: CA, CO, MA, NJ, OK, PA, SC, MD
- Vast majority were adopted in haste after the COVID-19 pandemic.

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- We next illustrate some of the consequences of these shortcomings, focusing on recent debates on:
 - Essential Personnel
 - Persons with Disabilities

- Many argue that essential personnel should receive priority under pandemic resource allocation systems.
- This view is also strongly endorsed by medical ethicists based on:
 - the backward-looking principle of reciprocity,
 - the forward-looking principle of instrumental value, and
 - due to the incentives it creates:

"... but giving them priority for ventilators [...] may also discourage absenteeism." (Emanuel et al. NEJM 2020)

- In an attempt to issue their guidelines in a timely manner during the COVID-19 crisis, some states remained vague about essential personnel priority, despite being precise on other dimensions.
- MA recommends a point system that relies on rigorous clinical criteria, but casually suggests "heightened priority" for essential personnel without detailing its implementation.
- The Pittsburgh guideline specifies two tie-breakers, one based on age and the other based on essential personnel status. However, it is silent on how to use these tie-breakers.
- The vagueness in these cases sharply contrasts with widely-accepted calls for clarity in rationing guidelines.

Confusion & Frustration due to Vague Descriptions

Who gets a ventilator? New gut-wrenching state guidelines issued on rationing equipment

Preference given to medical personnel, people who are healthy, younger

By Liz Kowalczyk Globe Staff, Updated April 7, 2020, 2:49 p.m.









I helped write Maryland's ventilator guidelines in 2017. Pa.'s rules are too vague. | Expert Opinion

Updated: April 27, 2020 - 11:33 AM

Darren P. Mareiniss, For The Inquirer





- Yet worse, states such as NY and MN had to give up on this consideration, largely due to concerns about extreme scenarios where no units remain for the rest of the society.
 - "[...] it is possible that they [essential personnel] would use most, if not all, of the short supply of ventilators; other groups systematically would be deprived access."

MN Pandemic Ethics Project, MN Dept. of Health 2010

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• "[...] may mean that only health care workers obtain access to ventilators in certain communities. This approach may leave no ventilators for community members, including children; this alternative was unacceptable to the Task Force."

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 Bottomline: A limitation of the allocation mechanism designed to implement these values resulted in giving up these values!

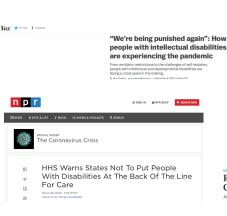
Opposition by Disabilities Advocates

- Disabilities advocates voice opposition to rationing plans based solely on survival probabilities.
 - Concern "based on well-founded fear of being sacrificed for the greater good" (Ne'eman 2020).
 - In their view, such criteria are inherently discriminatory and undermine public trust.

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 - Concern "based on well-founded fear of being sacrificed for the greater good" (Ne'eman 2020).
 - In their view, such criteria are inherently discriminatory and undermine public trust.
- Some groups instead prefer random selection for all units (Persad 2020).
- However, random selection for all units excludes several other ethical values.

Opposition by Disabilities Advocates







Rationing Plans in Coronavirus Crisis Draw Growing Discrimination Complaints

Advocacy groups say state guidelines illegally deprive people based on age, mental cognition or disability

Forbes associates innovation Laudership Money Sustress Small Business

The Disability Community Fights Deadly Discrimination Amid The COVID-19 Pandemic

Amid The COVID-19 Pande

Andrew Pulrang Constitutes O
Obserby & Inclusion
Exploring disability practions, publics, pullities, and culture.

Disability Discrimination Complaint Filed Over COVID-19 Treatment Rationing Plan in Washington State

March 23, 2020 / in From the Frontlines, Press Releases, Public Policy / by Pam Katz

Increasing Flexibility with a Reserve System

- It is clear that many challenges stem from the fact that a priority point system relies on a single priority ranking of patients that is identical for all units.
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- It is clear that many challenges stem from the fact that a priority point system relies on a single priority ranking of patients that is identical for all units.
 - A remedy has to break this limiting characteristic.
- A reserve system divides resources into multiple categories and uses different criteria for allocation of units in each category.
- These category-specific criteria reflect the balance of ethical values guiding allocation of units in the given category.

Real-Life Applications of Reserve Systems

- Deceased donor kidney allocation in the US
 Categories: Higher quality kidneys (20%), other kidneys (80%)
- Assignment of slots for Boston and NYC marathons
- H-1B visa allocation in the US
- School choice
 - Boston
 - Chicago
 - New York
 - Chile
- Affirmative Action in India
- College Admissions in Brazil

Reserve System: A Simple Idea

Primitives:

- 1. Division of the total supply of resources into multiple categories
- 2. The size of each category
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- In many applications, one may also need to specify what to do when a patient qualifies for a unit through multiple reserve categories.
 - Since units are homogenous, the patient does not care about the category through which she receives a unit.
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- In many applications, one may also need to specify what to do when a patient qualifies for a unit through multiple reserve categories.
 - Since units are homogenous, the patient does not care about the category through which she receives a unit.
 - However, this choice influences the outcome for other patients.
- This last point is often misunderstood in real-life applications:
 - Boston schools 50-50 neighborhood reserve (Dur et al. 2018)
 - H-1B visa allocation (Pathak et al. 2020)

Theoretical Agenda

- We therefore present a general theory of reserve systems
- Plan:
 - Propose three intuitive axioms and examine their implications
 - Formulate cutoff equilibrium solution concept, linking axioms to real-world
 - Show multiplicity of equilibrium and a way to compute
 - Examine sequential reserve matching policies which dominate practical applications
 - Introduce and analyze smart reserve matching policies

Formal Model

- I: set of patients each in need of one unit
- q: # of identical medical units in short supply
- C: set of reserve categories
- r_c : # of units subject to category-c allocation criteria s.t.

$$\sum_{c\in\mathcal{C}}r_c=q$$

- π_c : priority order of patients for units in category c
 - $i \pi_c j$ Patient i has higher priority for category-c units than patient j
 - $i \pi_c \emptyset$ Patient i is eligible for category c
 - \emptyset π_c c Patient i is ineligible for category c

 $\underline{\pi}_c$: weak order induced by π_c

Outcome and Properties

• A matching $\mu:I\to\mathcal{C}\cup\{\emptyset\}$ is an assignment of each patient to either a category or \emptyset such that no category is assigned to more patients than its size

 $\mu(i) = c$ Patient *i* receives a unit reserved for category *c*

 $\mu(i) = \emptyset$ Patient remains unmatched

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- ullet μ is non-wasteful if no unit from any category remains idle while there is a patient who is both unmatched and eligible for the category
- \bullet μ respects priorities if no patient ever remains unmatched while another patient with lower priority at some category receives a unit through that category

Cutoff Equilibrium

- We next introduce a natural counterpart of the standard competitive equilibrium for our model
- For any category $c \in \mathcal{C}$, a cutoff f_c is an element of $I \cup \{\emptyset\}$ s.t.

$$f_c \underline{\pi}_c \emptyset$$

- Expressed in terms of "cutoff" individual
- A cutoff plays the role of a non-negative price
- For a given a cutoff vector $f = (f_c)_{c \in \mathcal{C}}$, the budget set of patient i is

$$\mathcal{B}_i(f) = \{c \in \mathcal{C} : i \underline{\pi}_c f_c\}$$

Characterization through Cutoff Equilibria

- A cutoff equilibrium is a cutoff vector-matching pair (f, μ) s.t.
 - 1. For any patient $i \in I$,
 - (a) $\mu(i) \in \mathcal{B}_i(f) \cup \{\emptyset\}$, and
 - (b) $\mathcal{B}_i(f) \neq \emptyset \implies \mu(i) \in \mathcal{B}_i(f)$.
 - 2. For any category $c \in \mathcal{C}$,

$$|\mu^{-1}(c)| < r_c \implies f_c = \emptyset.$$

Here.

- the first condition corresponds to utility maximization within the budget set, whereas
- the second one corresponds to the market-clearing condition.

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- the second one corresponds to the market-clearing condition.
- A matching μ is a cutoff matching if it is supported by some cutoff vector f at a cutoff equilibrium (f, μ) .
- Theorem 1. A matching complies with eligibility requirements, is non-wasteful, and respects priorities if, and only if, it is a cutoff matching.

Cutoff Equilibria in Real-Life Applications

- It is widespread practice to describe the outcome of a reserve system through its cutoff equilibrium, often utilizing a metric that is used to construct the priority order at each category.
- India-Allocation of public jobs and seats at public schools:
 - Outcome defined by cutoff exam scores for each category.
- Chicago-Admission to Selective Enrollment High Schools:
 - Outcome defined by cutoff composite scores for the merit-only seats and for each of the four socioeconomic tiers.
- US-Assignment of H-1B visas:
 - 2005-2008: Outcome defined by cutoff application arrival dates for the general category and the advanced degree category (with ties broken with an even lottery within each category).

Cutoff Equilibria in Real-Life Applications

RAJASTHAN PUBLIC SERVICE COMMISSION, AJMER

DATE: 23-11-2012

THE CANDIDATES BEARING THE FOLLOWING ROLL NO. FOR THE RAJASTHAN STATE & SUBORDINATE SERVICES COMBINED COMPETTIVE (PRELIMINARY) EXAMINATION, 2012 HELD ON 1446-2012 ARE DECLARED PROVISIONALITY QUALIFIED FOR ADMISSION TO THE MAIN EXAMINATION IF ANY ADMIDIATE IS FOUND THAT HEISHE DOES NOT FULFILL THE CONDITIONS OF ELIGIBLITY PRESCRIBED AS PER ADVERTISEMENTIFULES, THE COMMISSION SHALL REJECT HISBERG CANDIDATIONS AT ANY STAGE.





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Cutoff Equilibria Properties

- We focus on \bar{f}_c^{μ}
 - Lowest π_c priority patient matched to category c (if exhausted)
- Lemma 1 shows that this is the maximum cutoff vector
 - ullet Value indicates selectivity of category: higher cutoff \Longrightarrow more competitive

Cutoff Equilibria Properties

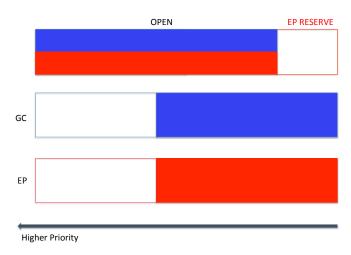
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 more competitive
- How do you find cutoff equilibrium matchings?
 - We start with a situation where we process categories sequentially.
 - Most widespread practice in real-life applications.

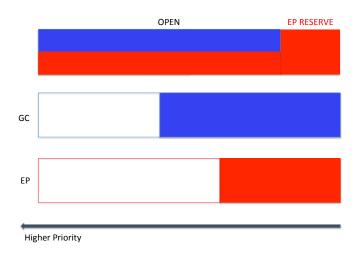
Sequential Category Processing: Open-Reserved



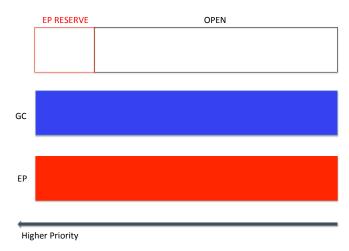
Sequential Category Processing: Open-Reserved



Open First - Reserved Next = Over & Above Policy



Sequential Category Processing: Reserved-Open



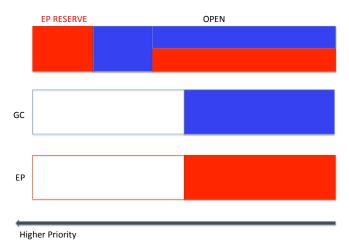
Sequential Category Processing: Reserved-Open



Sequential Category Processing: Reserved-Open



Reserved First - Open Next = Minimum Guarantee Policy



Construction of Cutoff Equilibria

• Example shows that there may be several cutoff matchings

Construction of Cutoff Equilibria

- Example shows that there may be several cutoff matchings
- We next present a procedure to construct all cutoff matchings
 - using the celebrated deferred acceptance algorithm (Gale & Shapley 1962)
 - on a hypothetical many-to-one matching market that relates to the original rationing problem.

Hypothetical Two-Sided Matching Market $\langle I, C, r, \pi, \succ \rangle$

- *I*: The set of patients
- C: The set of categories
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• Observation: All primitives except the student preferences naturally follow from the primitives of the original problem.

Individual-Proposing Deferred Acceptance Algorithm

• Step 1:

- Each patient applies to her most preferred acceptable category.
- Each category holds eligible applicants with highest priority up to capacity and rejects others.

• Step k:

- Each patient who was rejected in the previous step applies to her next preferred acceptable category.
- Considering all patients on hold and the new applicants, each category holds applicants with highest priority up to capacity and rejects others.
- The algorithm terminates when there are no rejections. All assignments on hold are finalized.

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- Theorem 2. A matching *complies with eligibility requirements*, is *non-wasteful*, and *respects priorities* if, and only if, it is DA-induced.
 - This result can be used to construct the set of cutoff equilibria or a selection from it

Sequential Reserve Matching

- The hypothetical two-sided matching market relies on an artificial preference profile $(\succ_i)_{i\in I}$ of patients over categories.
 - Patient i is considered for her eligible categories in sequence, following the ranking of these categories under her artificial preferences \succ_i .

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- Critically, this sequence can differ between patients.
 - Example: Patient A can be considered first for open category and then for Essential Personnel category, whereas patient B who has similar attributes can be considered for these categories in the reverse order.

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- Critically, this sequence can differ between patients.
 - Example: Patient A can be considered first for open category and then for Essential Personnel category, whereas patient B who has similar attributes can be considered for these categories in the reverse order.
- Without a systematic way to construct these preferences, it may be difficult to motivate this methodology for real-life implementation.

Sequential Reserve Matching: Processing Categories

- Not all reserve systems have to process categories sequentially, but in most real-life practices they do.
- An order of precedence ▷ is a linear order over the set of categories C, interpreted as the processing sequence of categories
 - $c \triangleright c'$: Category-c units are to be allocated before category-c' units

Sequential Reserve Matching: Processing Categories

- Sequential Reserve Matching: Fix a processing sequence ▷ of the categories. Following this sequence, allocate units in each category to highest priority patients using category-specific priorities.
 - In previous example, in the first case all open units are processed first (over-and-above), and in the second case all reserve units processed first (minimum guarantee).

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 - In previous example, in the first case all open units are processed first (over-and-above), and in the second case all reserve units processed first (minimum guarantee).
- Proposition 1. Fix an order of precedence ▷. Let the preference profile \succ^{\triangleright} be such that for each patient i and pair of categories c, c',

$$c \succ_i^{\triangleright} c' \iff c \triangleright c'.$$

Then the resulting sequential reserve matching φ_{\triangleright} is DA-induced from the preference profile \succ^{\triangleright} .

Category Processing and Cutoff Comparative Static

- Proposition 2. Fix a pair of categories $c, c' \in \mathcal{C}$ and a pair of orders of precedence $\triangleright, \triangleright' \in \Delta$ such that:
 - $c' \triangleright c$.
 - $c \triangleright' c'$, and
 - for any $\hat{c} \in \mathcal{C}$ and $c^* \in \mathcal{C} \setminus \{c, c'\}$

$$\hat{c} \triangleright c^* \iff \hat{c} \triangleright' c^*.$$

That is, \triangleright' is obtained from \triangleright by only changing the order of c with its immediate predecessor c'. Then,

$$\overline{f}_c^{\varphi_{\triangleright'}} \ \underline{\pi}_c \ \overline{f}_c^{\varphi_{\triangleright}}$$

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• Interpretation: The earlier a category is processed, the more selective it becomes.

Reserve Systems with a Baseline Priority Order

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 - π_c : Prioritizes beneficiaries of category c over others and π_u is used to break ties internally within the two groups.
- General-community patients I_g are patients who are beneficiaries of the unreserved category only.

Comparative Statics: Order of Precedence

- Proposition 3. Assuming there are at most five categories and each patient is a beneficiary of at most one preferential-treatment category, consider a soft reserve system induced by a baseline priority order. Fix a preferential treatment category $c \in \mathcal{C} \setminus \{u\}$, any other category $c' \in \mathcal{C} \setminus \{c\}$, and a pair of orders of precedence $\triangleright, \triangleright' \in \Delta$ such that:
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• Interpretation: The later a preferential-treatment category is processed, the better for its beneficiaries.

• Example 2: There is a single-unit unreserved category u, a single-unit preferential-treatment category c, and two agents i_1, i_2 . The baseline priorities are s.t.

$$i_1 \pi_u i_2 \pi_u \emptyset$$

and the sole beneficiary of category c (which has hard reserves) is individual i_1 . Hence:

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• i_1 receives the unreserved unit and category-c unit is left idle.

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Case2 (Efficient Reserve Processing): $c \triangleright' u$

• i_1 receives the category-c unit and i_2 receives the unreserved unit.

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Case2 (Efficient Reserve Processing): $c \triangleright' u$

- i_1 receives the category-c unit and i_2 receives the unreserved unit.
- Issue with Case 1: The more flexible unreserved unit is allocated to patient i₁, who is the only beneficiary of category c; this results in suboptimal utilization of reserves.

• Example 3: There is a single-unit unreserved category u and two single-unit preferential-treatment categories d, e. There are four agents i_1 , i_2 , i_3 , i_4 .

The baseline priorities are s.t.

$$i_1 \pi_u i_2 \pi_u i_3 \pi_u i_4 \pi_u \emptyset.$$

The beneficiaries for the two preferential-treatment categories are $I_d = \{i_2, i_4\}$ and $I_e = \{i_2, i_3\}$, and the reserves are soft. Hence:

$$i_2 \pi_d i_4 \pi_d i_1 \pi_d i_3 \pi_d \emptyset$$
 and $i_2 \pi_e i_3 \pi_e i_1 \pi_e i_4 \pi_e \emptyset$.

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Case 2 $(d \triangleright' e \triangleright' u)$: i_2 receives the category-d unit, i_3 receives the category-e unit, and i_1 receives the unreserved unit.

• Issue with Case 1: Higher baseline priority i_3 is rejected at the expense of lower baseline priority i_4 due to mechanical reserve processing.

Maximality in Beneficiary Assignment

- The following requirement helps us to avoid any efficiency loss by precluding the myopic assignment of patients to categories.
- ullet A matching $\mu \in \mathcal{M}$ is maximal in beneficiary assignment if

$$\mu \in \arg\max_{\nu \in \mathcal{M}} \left| \cup_{c \in \mathcal{C} \setminus \{u\}} \left(\nu^{-1}(c) \cap I_c \right) \right|$$

 Observation: Together with non-wastefulness, maximality in beneficiary assignment implies Pareto efficiency.

- Intuition: The main idea is, determining which agents are to be matched (with some category) in a greedy manner following their baseline priorities while assuring maximality in beneficiary assignment.
- This can be done in multiple ways, depending on when unreserved units are processed.
- If all unreserved units are processed at the end, this extreme case of our algorithm gives us a minimum guarantee version of the smart reserve matchings.
- If all unreserved units are processed at the beginning, this other extreme of our algorithm gives us an over & above version of the smart reserve matchings.

• Proposition 4. Any smart reserve matching complies with eligibility requirements, is non-wasteful, respects priorities and maximal in beneficiary assignment.

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- Theorem 3. Let ω , μ be any over & above and minimum guarantee smart reserve matching respectively. Moreover let ν be any matching that complies with eligibility requirements, is non-wasteful, respects priorities and maximal in beneficiary assignment. Then

$$\overline{f}_{\mu}^{\omega} \underline{\pi}_{\mu} \overline{f}_{\mu}^{\nu} \underline{\pi}_{\mu} \overline{f}_{\mu}^{\mu}$$

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$$\overline{f}_u^{\omega} \underline{\pi}_u \overline{f}_u^{\nu} \underline{\pi}_u \overline{f}_u^{\mu}$$

• Interpretation: Of all matchings that complies with eligibility requirements, is non-wasteful, respects priorities and maximal in beneficiary assignment, over & above smart matchings are the most selective and minimum guarantee smart matchings are the least selective for unreserved category.

Most Related Literature

- Reserve Systems: Hafalir, Yenmez & Yildirim (TE 2013),
 Echenique & Yenmez (AER 2015)
- Sequential Reserve Matching: Kominers & Sönmez (TE 2016)
- Smart Reserves: Sönmez and Yenmez (2020)
- Impact of Reserve Processing Sequence: Dur, Kominers, Pathak & Sönmez (JPE 2018), Dur, Pathak & Sönmez (JET 2020),
 Sönmez & Yenmez (2019), Pathak, Rees-Jones & Sönmez (2020)
- Additional Applications: Aygün and Bó (2016), Aygün and Turhan (2016, 2017), Correa et. al (2019)

Reserve System in Pittsburgh (UPMC)

A MODEL HOSPITAL POLICY FOR FAIR ALLOCATION OF MEDICATIONS TO TREAT COVID-19

HOME (/) • A MODEL HOSPITAL POLICY FOR FAIR ALLOCATION OF MEDICATIONS TO TREAT COVID-15



Available now online:

To assist hospitals and health systems to implement a transparent and fair approach to allocate scarce medications to treat patients with COVID-19, we have created a model hospital policy and allocation framework. Hospitals and health systems are welcome to adapt the policy for their specific needs. Click here to download a PDF (https://ccn.pitt.edu/sites/default/files/2020-05-

- Designed by a team of diversity and inclusion experts, ethicists, economists, and medical specialists from the University of Pittsburgh, Harvard University, University of Denver, Boston College and MIT.
- "The model policy uses a weighted lottery or categorial reserve system to fairly allocate drug supplies if there is insufficient supply to treat all eligible patients."

Pittsburgh Model Policy for Anti-Viral Medications

- Reserve categories based on the combinations of the following three considerations:
 - Hardest hit (ADI of 8-10)
 - Essential worker (using PA state definition)
 - Is patient expected to die in one-year?
- Priorities are based on lottery
 - In this case, reserve system simplifies to stratified lottery (25% boost for each of the first two considerations, 50% reduction for the third)
 - Used for week of May 25th for Remdesivir
 - Outcome determined dynamically through cutoff lottery points for each category
- After its initial deployment at UPMC in May 2020, endorsed by the Commonwealth of Pennsylvania.

- July 2020: CDC and NIH commissioned the National Academies of Sciences, Engineering, and Medicine (NASEM) to formulate their recommendations on the equitable allocation of a COVID-19 vaccine.
 - An ad hoc committee is formed.
- September 2020: A discussion draft of the preliminary Framework for Equitable Allocation of COVID-19 Vaccine is made public.
 - Comments from the public is solicited.
 - In his written and oral comments, University of Pennsylvania bioethicist Harald Schmidt have formally inquired the precise mechanism recommended to prioritize members of hard-hit communities, and brought our proposed reserve system to the committee's attention.

September 2020: In response to the NASEM discussion draft, JAMA published the viewpoint "Fairly Prioritizing Groups for Access to COVID-19 Vaccines," endorsing our proposed reserve system (Persad, Peek & Emanuel 2020).

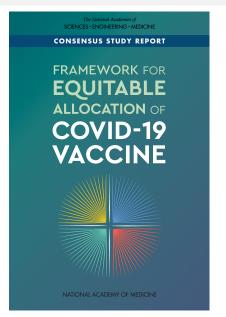
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"Dividing the initial vaccine allotment into priority access categories and using medical criteria to prioritize within each category is a promising approach. For instance, half of the initial allotment might be prioritized for frontline health workers, a quarter for people working or living in high-risk settings, and the remainder for others. Within each category, preference could be given to people with high-risk medical conditions. Such a categorized approach would be preferable to the tiered ordering previously used for influenza vaccines, because it ensures that multiple priority groups will have initial access to vaccines."

 October 2020: NASEM published their final Framework for Equitable Allocation of COVID-19 Vaccine (2020), based on the ethical values formulated in (Emanuel et al. 2020), whose lead authors later on endorsed our proposed reserve system.

"Fair Allocation of Scarce Medical Resources in the Time of COVID-19

In May 2020, an article in The New England Journal of Medicine proposed a set of ethical values to underpin recommendations for allocating scarce medical resources during the COVID-19 pandemic (Emanuel et al. NEJM 2020). Drawing on previous proposals about how to allocate resources during scenarios of absolute scarcity, such as pandemics, the authors identify four fundamental ethical values: (1) maximize benefit, (2) treat people equally, (3) promote and reward instrumental value (i.e., providing benefit to others), and (4) give priority to the worst off."



 The final NASEM framework formally recommends a 10 percent reserve for people from hard-hit areas.

"The committee does not propose an approach in which, within each phase, all vaccine is first given to people in high SVI areas. Rather the committee proposes that the SVI be used in two ways. First as previously noted, a reserved 10 percent portion of the total federal allocation of COVID-19 vaccine may be reserved to target areas with a high SVI (defined as the top 25 percent of the SVI distribution within the state)."

Conclusion

- In the first few months of the COVID-19 pandemic, many societies were caught unprepared when they needed guidelines for a possible ventilator rationing.
- At present, there is a worldwide need for policies and mechanisms for vaccine allocation.
- Poorly designed rationing mechanisms may damage the social contract between different segments of the society.
- Widely accepted but potentially competing ethical values for pandemic rationing require an allocation mechanism to implement the desired balance of values.
- Finding the right mechanism to honor these principles is therefore important for maintaining the social fabric.

Conclusion

- Because the mechanism is a tool to realize ethical values and not an end in itself, it should permit a wide range of options.
- The exclusion or inadequate balancing of certain ethical principles may do more harm than good.

"Maybe you end up saving more people but at the end you have got a society at war with itself. Some people are going to be told they don't matter enough."

Quote attributed to Christina Pagel in New York Times

 When revising or modifying guidelines during or after the COVID-19 pandemic, a reserve system should be part of the arsenal.